NONLINEAR PHENOMENA IN ELECTROMAGNETIC AND ACOUSTIC WAVE PROPAGATION(U) STANFORD UNIV CA DEPT OF MATHEMATICS JB KELLER APR 84 ARO-17902. 40-MA DAAG29-81-K-0032 F/G 20/14 AD-8148 716 1/1 UNCLASSIFIED NL



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Nonlinear Phenomena in Electromagnetic and Acoustic Wave Propagation

Final Report

January 15, 1981 — January 14, 1984

Professor Joseph B. Keller
April 1984

U.S. Army Research Office Contract: DAAG29-81-K-0032



Stanford University

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Nonlinear Phenomena in Electromagnetic and Acoustic Wave Propagation

FINAL REPORT

January 15, 1981 - January 14, 1984

1. Statement of the problems studied

We have studied mathematical problems in electromagnetic and acoustic wave propagation which involve nonlinear partial differential equations, or linear partial differential equations with random coefficients.

2. Summary of the most important results

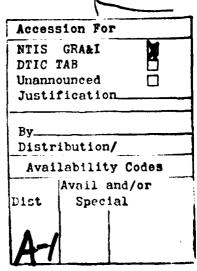
A general theory of weakly nonlinear high frequency wave propagation was developed which applies to waves in any number of dimensions. It justifies the nonlinearization technique of Whitham and Landau and extends it to interacting waves and to other types of waves. The theory was successfully applied to weak shock diffraction.

The theory of wave reflection from rough surfaces was extended to yield the correlation functions of the scattered field. It was found that the second order correlations could be expressed in terms of the reflection coefficient and the differential scattering cross section of the surface.

Many other problems were analyzed successfully.

- 3. List of papers published and submitted for publication
 See Attachment A.
- 4. <u>List of scientific personnel</u>

See Attachment B.



Attachment A.

29.	J. B. Keller	Temperley's model of gas condensation Pub: J. Chem. Phys., 74, 4203-4204, 1981.
30.	J. B. Keller J. G. Watson	Kelvin wave production <u>Pub</u> : J. Phys. Ocean., <u>11</u> , 284-285, 1981.
31.	J. B. Keller S. I. Rubinow	Recurrent precipitation and Liesegang rings Pub: J. Chem. Phys., 74, 5000-5007, 1981.
32.	J. B. Keller M. J. Miksis JM. Vanden-Broeck	Axisymmetric bubble or drop in a uniform flow Pub: J. Fluid Mech., 108, 89-100, 1981.
33.	JM. Vanden-Broeck	Numerical calculation of standing waves in water of arbitrary uniform depth Pub: Phys. Fluids, 24, 812-815, 1981.
34.	R. E. Caflisch K. C. Nunan	Evaluation of a function at infinity from its power series Pub: Phys. Rev. Letters, 46, 1255-1256, 1981.
35.	J. B. Keller D. M. Levy D. S. Ahluwalia	Internal and surface wave production in a stratified fluid Pub: Wave Motion, 3, 215-229, 1981.
36.	R. E. Caflisch J. B. Keller	Quench front propagation Pub: Nuc. Eng. Design, 65, 97-102, 1981.
37.	M. J. Miksis	A bubble in an axially symmetric shear flow Pub: Phys. Fluids, 24, 1229-1231, 1981.
38.	JM. Vanden-Broeck	Deformation of a liquid surface by an impinging gas jet Pub: SIAM J. Appl. Math., 41, 306-309, 1981.
39.	J. B. Keller	Oblique derivative boundary conditions and the image method Pub: SIAM J. Appl. Math., 41, 294-300, 1981.

40.	R. Burridge J. B. Keller	Poroelasticity equations derived from microstructure
		<u>Pub</u> : J. Acoust. Soc. Am., <u>70</u> , 1140-1146, 1981.
41.	J. C. Neu	Stochastically perturbed resonance
		<u>Pub</u> : SIAM J. Appl. Math., <u>41</u> , 365-369, 1981.
42.	M. J. Miksis	Shape of a drop in an electric field
		<u>Pub</u> : Phys. Fluids, <u>24</u> , 1967-1972, 1981.
43.	JM. Vanden-Broeck	The influence of capillarity on cavitating flow past a flat plate
		Pub: Quart. J. Mech. Appl. Math., 34, 465-473, 1981.
44.	A. Jeffrey J. Mvungi	A note on the effect of submerged obstacles on water waves in a channel
-		<u>Pub</u> : J. Appl. Math. Phys., <u>32</u> 756-763, 1981.
45.	P. S. Hagan	Target patterns in reaction-diffusion systems
		<u>Pub</u> : Adv. Appl. Math., 2, 400-416, 1981.
46.*	P. S. Hagan M. S. Cohen	Diffusion-induced morphongenesis in the development of <u>Dictyostelium</u>
		Pub: J. Theor. Biol., 93, 881-908, 1981.
47.	P. S. Hagan	Nuclear magnetic-resonance studies of cation-
	D. Z. Ting J. D. Doll	ransport across vesicle bilayer membranes Pub: Biophys. J., 34, 189-214, 1981.
		<u>rab.</u> blophys. 5., <u>54,</u> 103-224, 1361.
48.	A. Jeffrey	A note on the multiple scale Fourier transform
r. Kawana	T. Kawahara	Pub: Nonlinear Anal., Theory, Methods and Applics., 5, 1331-1340, 1981.
49.	J. C. Neu	A nonlinear analysis of interfacial waves
		Acc: Phys. Fluids, in press.

^{*}Not supported by AFOSR or ONR.

50.	J. B. Keller	Optimum inspection policies
		Pub: Management Sci., 28, 447-450, 1982.
51.	P. S. Hagan	Travelling and stacked travelling wave solutions of parabolic equations
		<u>Pub</u> : SIAM J. Math. Anal., <u>13</u> , 717-738, 1982.
52.	JM. Vanden-Broeck	Contact problems involving the flow past an inflated aerofoil
		<u>Pub</u> : J. Appl. Mech., <u>49</u> , 263-265, 1982.
53.	JM. Vanden-Broeck	Nonlinar two-dimensional sail theory
		Pub: Phys. Fluids, 25, 420-423, 1982.
55. P. S. Hagan	P. S. Hagan	Spiral waves in reaction diffusion equations
		Pub: SIAM J. Appl. Math., 42, 762-786, 1982.
56.	JM. Vanden-Broeck J. B. Keller	Parabolic approximations for ship waves and wave resistance
		Pub: Proceedings of the Third International Conference on Numerical Ship Hydrodynamics, Paris, France, June 16-19, 1981.
57.		Asymptotic Methods in Nonlinear Wave Problems
	T. Kawahara	Pub: Pitman Publishing, Ltd., London, 1982.
58.	M. J. Miksis	Rising Bubbles
	JM. Vanden-Broeck J. B. Keller	<u>Pub</u> : J. Fluid Mech., <u>123</u> , 31-42, 1982.
59.	J. C. Neu	Resonantly interacting waves
		<u>Pub</u> : SIAM J. Appl. Math., 43, I, 141-156, 1983.
	J. B. Keller	Surface tension driven flows
	M. J. Miksis	<u>Pub</u> : SIAM J. Appl. Math., <u>43</u> , II, 268-277, 1983.
61.	A. Jepson A. Spence	Folds in solutions of two parameter systems and their calculation: Part I
		Pub: Stanford Univ. Numer. Anal. Report, 82-02.

62.	J. B. Keller	Time-dependent queues
		<u>Pub</u> : SIAM Rev., <u>24</u> , 401-412, 1982.
63. R. E. Caflisch B. Nicolaenko	R. E. Caflisch	Shock profile solutions of the Boltzmann equation
	B. Nicolaenko	Pub: Comm. Math. Phys., 86, 161-194, 1982.
64.	P. S. Hagan R. E. Caflisch	Arrow's model of optimal pricing, use and exploration of undertain natural resources
	J. B. Keller	Sub: Econometrica
65.	R. E. Caflisch	Radiation transport in a hot plasma
		Acc: SIAM J. Appl. Math., in press.
66.	J. B. Keller	Jets rising and falling under gravity
JM. Vanden-Broeck	JM. Vanden-Broeck	<u>Pub:</u> J. Fluid Mech., <u>124</u> , 335-345, 1982.
67.	R. E. Caflisch	Fluid dynamics and the Boltzmann equation
		<u>Pub</u> : Stud. Stat. Mech., <u>5</u> , 194-223, 1983.
M Seul	M Seul	Theory of periodic structures in lipid bilayer membranes
	H. L. Frisch H. M. McConnell	<u>Pub</u> : Proc. Nat. Acad. Sci., <u>79</u> , 3918, 1982.
69.	R. E. Caflisch	The fluid-dynamic limit of a model Boltzmann equation in the presence of a shock
		<u>Pub</u> : Institute National de Recherche en Informatique et en Automatique, INRIA No. 81, June 1981, 1-34.
70.	P. F. Rhodes-Robinson	On the short surface waves due to half-immersed circular cylinder oscillating on water of infinite depth
		Pub: Proc. Royal Soc. London A, 384, 333-357, 1982.

Note on the reflexion of water waves at a wall in the presence of surface tension

92, 369-373, 1982.

Pub: Math. Proc. Cambridge Philosophical Soc.,

71. P. F. Rhodes-Robinson

^{*}Not supported by AFOSR or ONR.

72.	P. F. Rhodes-Robinson	On the generation of water waves at an inertial surface
		Acc: J. Australian Math. Soc. B, in press.
73.	R. E. Caflisch G. C. Papanicolaou	Dynamic theory of suspensions with Brownian effects
		Pub: SIAM J. Appl. Math., 43, No. 4, 1983.
74. R. E. Caflisch G. C. Papanicolaou		Instability in settling of suspensions due to Brownian effects
		Pub: Proceedings of conference Two-Phase Flow.
75.	R. E. Caflisch B. Nicolaenko	Shock waves and the Boltzmann equation
	B. MICOLEGUED	Pub: Proceedings NSF-AMS conference non-linear PDE.
76. J. H. Maddocks	Restricted quadratic forms and their application to bifurcation and stability in constrained variational principles	
		Acc. SIAM J. Appl. Math.
77.	M. S. Falkovitz L. A. Segel	Spatially inhomogeneous polymerization in unstirred bulk
		Pub: SIAM J. Appl. Math., 43, 386-416, 1983.
78. M. S. Falkovitz J. L. Frisch		The scale of non-homogeneity as defined by diffusion measurements
		Pub: Journal of Membrane Science, 10, 61, 1982.
79.	M. S. Falkovitz H. L. Frisch	Optimal catalyst distribution in a membrane
	J. B. Keller	Pub: Chem. Eng. Sci., 39, No 3, 601-604, 1984.
80.*	M. S. Falkovits	Crawling of Worms
J. B. Keller	<u>Pub</u> : J. Theor. Biol., <u>104</u> , 417-442, 1983.	
81.	A. Jeffrey J. Mvungi	The random choice method and the free-surface water profile after the collapse of a dam wall
		Pub: Wave Motion, 4, 381-389, 1982.

^{*}Not supported by AFOSR or ONR.

82.	J. G. Watson E. L. Reiss	A statistical theory for imperfect bifurcation
	E. L. REISS	<u>Pub</u> : SIAM J. Appl. Math., <u>42</u> , 135-148, 1982.
83.	J. G. Watson	Reflection, scattering and absorption of acoustic
	J. B. Keller	waves by rough surfaces
		<u>Pub</u> : J. Acoust. Soc. Am., 74, 1887-1894, 1983.
84.	M. I. Weinstein	Global existence for a generalized Korteweg - de Vries equation
		Sub: SIAM J. Math. Anal.
85.	M. I. Weinstein	Nonlinear Schrödinger equations and sharp interpolation estimates
		Pub: Commun. Math. Phys., 87, 567-576, 1983.
86.	M. Cheney	Two-dimensional scattering: the number of
	na oladay	bound states from scattering data
		Sub: J. Math. Phys.
87.	L. L. Bonilla A. Liñán	Relaxation oscillations, pulses, and travelling waves in the diffusive Volterra delay-differential
		equation Acc: SIAM J. Appl. Math., in press.
88.	P. F. Rhodes-Robinson	Note on the effect of surface tension on water waves at an inertial surface
		<u>Pub</u> : J. Fluid Mech., <u>125</u> , 375-377, 1982.
89.	J. B. Keller	Weak shock diffraction
	J. Hunter	<u>Pub</u> : Wave Motion, <u>6</u> , 79-89, 1984.
90.	J. B. Keller	Weakly nonlinear high frequency waves
	J. Hunter	<u>Pub</u> : Comm. Pure Appl. Math., <u>36</u> , 547-569, 1983.
91.	J. B. Keller	Asymptotic analysis of a viscous Cochlear model
	J. C. Neu	Sub: J. Acoust. Soc. Am.
92.	J. B. Keller	Parabolic approximations for ship waves and wave

resistance

Pub: Proc. 3rd Intl. Conf. on Numerical Ship

Hydrodynamics, Paris, France, June 16-19, 1981.

J.-M. Vanden-Broeck

93.	A. Spence A. Jepson	The numerical computation of turning points of nonlinear equations
		Pub: Treatment of Integral Equations by Numerical Methods, 169-183, London, 1982.
94.	J. B. Keller	Biot's poroelasticity equations by homogenization
	R. Burridge	Pub: Springer Lecture Notes, in Macroscopic Properties of Disordered Media, NY, 51-57,1982.
95.	J. B. Keller	Capillary waves on a vertical jet
		Pub: J. Fluid Mech., 135, 171-173, 1983.
96.	J. B. Keller	Survival estimation using censored data
A. S. Whittemore	Sub: J. Royal Statist. Soc., Series B	
97.	J. B. Keller J. F. Geer	Eigenvalues of slender cavities and waves in slender tubes
		Pub: J. Acoust. Soc. Am., 74, 1895-1904, 1983.
98.	J. B. Keller	Valuation of stocks and options
	R. Voronka	To be submitted.
99.	M. Cheney	Inverse scattering in dimension two
		Acc: J. Math. Phys., in press.
100.	K. C. Nunan	Effective viscosity of a periodic suspension
	J. B. Keller	Acc: J. Fluid Mech., in press.
101.	K. C. Nunan	Effective elasticity Tensor of a Periodic Composite
<i>(</i> :\	J. B. Keller	Acc: J. Mech. Phys. Solids, in press.
102.	J. B. Keller	Breaking of liquid films and threads
		<u>Pub</u> : Phys. Fluids, <u>26</u> , 3451-3453, 1983.
103.	J. B. Keller	Hanging rope of minimum elongation
	G. R. Verma	Acc: SIAM Rev., in press.

104.	M. Cheney S. Coen	Velocity & density of a two-dimensional acoustic medium from point source surface data
	A. Weglein	Sub: Phys. Rev. Lett.
105.	J. B. Keller	Probability of a shutout in racquetball
		Acc: SIAM Rev., in press
106.	S. Venakides	The Zero Dispersion Limit of the Korteweg-de Vries Equation for Initial Potentials with Non-trivial Reflection Coefficient
		Acc: Comm. Pure Appl. Math.
107.	J. H. Maddocks	Stability of Nonlinearly Elastic Rods
		Acc: Arch. Rat. Mech. Anal., in press.
108.	J. B. Keller	Genetic Variability Due to Geographical Inhomogeneity
		Sub: J. Math. Biol.
109.	J. B. Keller M. S. Falkovitz	Precipitation pattern formation
		In preparation.
110.	V. Twersky	Scattering and Nonscattering Obstacles
		Pub: SIAM J. Appl. Math., 43, No 4, 1983.
111.	R.E. Caflisch	Nonlinear Dynamical Theory of the Elastica
	J.H. Maddocks	Sub: Proc. Roy. Soc. Edin.
112.	J.B. Keller	Rough Surface Scattering via the Smoothing Method
	J.G. Watson	Acc: J. Acoust. Soc. Am.
113.	J.B. Keller	Free boundary problems in mechanics
		Acc: Lectures in Partial Differential Equations S.S. Chern, editor, Springer New York, in press.
114.	J.B. Keller	Newton's second law

Am. J. Physics

Sub:

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Attachment B.

Army contract DAAG29-81-K-0032

Scientific Personnel, January 15, 1981 through January 14, 1984:

Russell E. Caflish

Jeanmarc Vanden Broeck

John G. Watson

Meira Falkovitz

John H. Maddocks

Margaret Cheney

Michael Weinstein

Graham P. Eatwell

Stephanos Venakides

John A. Fawcett

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